

1. The total surface area of a cube is 294 cm^2 .

Work out the volume of the cube.

$$SA = 6 \times x^2$$

↑
length of side

$$6x^2 = 294$$

$$\div 6 \quad \div 6$$

$$x^2 = 49$$

$$\sqrt{\quad} \quad \sqrt{\quad}$$

$$x = \sqrt{49}$$

$$x = 7$$

$$6 \overline{) 294} \begin{array}{r} 049 \\ \underline{294} \\ 0 \end{array}$$

$$\text{Volume} = \text{length} \times \text{width} \times \text{height}$$

$$\text{Volume} = 7 \times 7 \times 7$$

$$= 49 \times 7$$

$$= 343 \text{ cm}^3$$

x	40	9
7	280	63

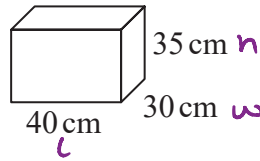
$$\begin{array}{r} 280 \\ 63+ \\ \hline 343 \\ \end{array}$$

(Total for Question is 4 marks)

..... 343 cm³

2. Chloe has a van.

She is going to use the van to deliver boxes.
Each box is a cuboid, 40 cm by 30 cm by 35 cm.



$1\text{ m} = 100\text{ cm}$

The space for boxes in the van has

- maximum length 2.4 m = 240 cm
- maximum width 1.5 m = 150 cm
- maximum height 1.4 m = 140 cm

The space for boxes is empty.
Chloe wants to put as many boxes as possible into the van.

She can put 3 boxes into the van in one minute.
Assume that the space for boxes is in the shape of a cuboid.

(a) Work out how many minutes it should take Chloe to put as many boxes as possible into the van.

$\frac{240}{40} = 6$ boxes along length

$\frac{150}{30} = 5$ boxes along width

$\frac{140}{35} = 4$ boxes along height ✓

$6 \times 5 \times 4 = 120$ ✓ boxes in van

3 boxes in 1 min
 $\downarrow \times 40$ $\downarrow \times 40$
 120 boxes in 40 mins ✓

..... 40 ✓ minutes
(4)

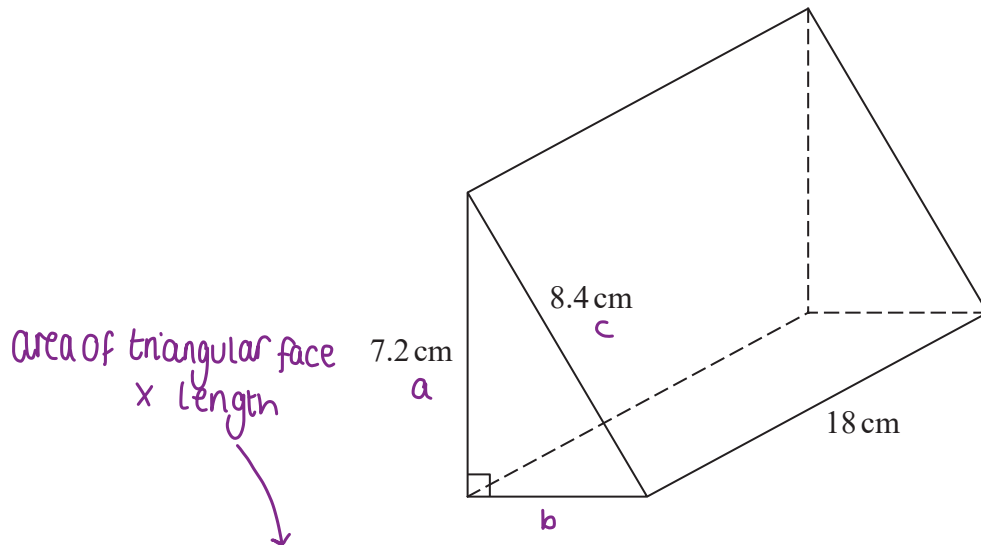
The space for boxes might **not** be in the shape of a cuboid.

(b) Explain how this could affect the time it would take Chloe to put as many boxes as possible into the van.

..... If boxes no longer fit along each edge, then less boxes may fit
 into the van, meaning it would take less time ✓
(1)

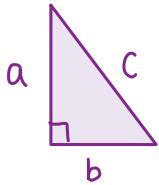
(Total for Question is 5 marks)

3. Here is a **triangular prism**.



Work out the **volume** of the prism.

Give your answer correct to **3 significant figures**.



Finding b (base of triangle):

$$a^2 + b^2 = c^2 \quad \leftarrow \text{Pythagorean theorem}$$

$$b^2 = c^2 - a^2$$

$$b^2 = 8.4^2 - 7.2^2 \quad \textcircled{1}$$

$$b^2 = 18.72$$

$$b = \sqrt{18.72} \quad \textcircled{1} \leftarrow \text{leave in exact form}$$

Area of triangle:

$$A = \frac{1}{2}bh$$

$$= \frac{1}{2} \times \sqrt{18.72} \times 7.2$$

$$= 15.57598... \quad \textcircled{1}$$

Volume of prism:

$$15.57598... \times 18 = 280.368... \quad \textcircled{1}$$

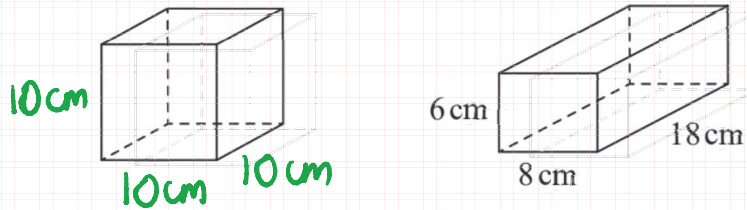
↑
use exact value

$3 < 5$ so round down
to 280 to 3 SF

..... 280 $\textcircled{1}$ cm^3

(Total for Question is 5 marks)

4. The diagram shows a cube and a cuboid.



The total surface area of the cube is equal to the total surface area of the cuboid.

Janet says,

“The volume of the cube is equal to the volume of the cuboid.”

Is Janet correct?

You must show how you get your answer.

SA cuboid:

$$6 \times 8 = 48 \text{ cm}^2$$

$$6 \times 18 = 108 \text{ cm}^2$$

$$8 \times 18 = 144 \text{ cm}^2$$

$$48 + 108 + 144 = 300 \text{ cm}^2 \text{ (1)}$$

$$300 \times 2 = 600 \text{ cm}^2 \text{ (1)}$$

Area of each face in cube must be the same

$$\therefore \text{area of one face} = \frac{600}{6} = 100 \text{ cm}^2$$

Length of each side in cube must be the same

Since area = 100 cm^2 each length must be 10 cm (1)
(because $10 \times 10 = 100$)

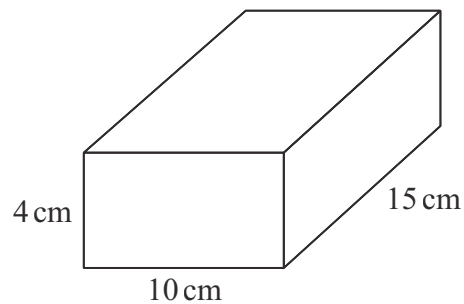
Volume of cube: $10 \times 10 \times 10 = 1000 \text{ cm}^3$

Volume of cuboid: $6 \times 8 \times 18 = 864 \text{ cm}^3$ (1)

← Volume = $h \times w \times d$

No Janet is not correct since $1000 \neq 864$ (1)

5. Here is a cuboid.



$$\begin{aligned}
 V &= L \times w \times d \\
 &= 10\text{cm} \times 4\text{cm} \times 15\text{cm} \\
 &\quad \times \begin{array}{r} 15 \\ 4 \\ \hline 60 \\ 2 \end{array}
 \end{aligned}$$

Work out the volume of the cuboid.

$$\begin{aligned}
 &= 10\text{cm} \times 60\text{cm}^2 \checkmark_1 \\
 &= 600\text{cm}^3 \checkmark_3
 \end{aligned}$$

..... 600 cm³ ✓

(Total for Question is 3 marks)